

$$4. \quad \frac{a^2(m^2+n^2)}{a(m^2-mn+n^2)} = \frac{a^2(m+n)(m^2-mn+n^2)}{a(m^2-mn+n^2)}$$

$$= a(m+n)$$

$$\frac{(x^2-xy+y^2)(x^2+xy+y^2)}{x^2(x^2+xy+y^2)+xy(x^2+xy+y^2)+y^2(x^2+xy+y^2)}$$

$$= \frac{(x^2-xy+y^2)(x^2+xy+y^2)}{(x+xy+y^2)(x+xy+y^2)} = \frac{x^2-xy+y^2}{x^2+xy+y^2}$$

$$x^0 \left(1 - \frac{x}{3} - \frac{x^2}{4} \right) \left| 1 - \frac{x}{2} \right. \left(1 - \frac{x}{6} + \frac{7x^2}{36} + \frac{5x^3}{216} + \frac{73x^4}{1296} + \dots \right)$$

$$\frac{-\frac{x}{6} + \frac{x^2}{4}}{1 - \frac{x}{3} - \frac{x^2}{4}}$$

$$\frac{-\frac{x}{6} + \frac{x^2}{18} + \frac{x^3}{24}}{\frac{7x^2}{36} - \frac{x^3}{108} - \frac{7x^4}{144}}$$

$$+ \frac{5}{216} + \frac{7x^4}{144} - \frac{5x^4}{648} - \frac{5x^5}{864}$$

$$\frac{73x^4}{1296} + \frac{5x^5}{864} - \frac{73x^4}{1296} - \frac{73x^5}{3888} - \frac{73x^6}{5184}$$

	$1 - \frac{1}{2}$
$\frac{1}{3}$	$\frac{1}{3}\alpha + \frac{1}{3}\beta + \frac{1}{3}\gamma + \frac{1}{3}\delta + \frac{1}{3}\epsilon + \dots$
$\frac{1}{4}$	$\frac{1}{4}\alpha + \frac{1}{4}\beta + \frac{1}{4}\gamma + \frac{1}{4}\delta + \dots$
1	$\alpha + \beta + \gamma + \delta + \epsilon + \dots$

$$\therefore \alpha = 1, \beta = -\frac{1}{2} + \frac{1}{3} = -\frac{1}{6}, \gamma = -\frac{1}{6} \times \frac{1}{3} + \frac{1}{4} = \frac{7}{36}$$

$$\delta = \frac{1}{3} \times \frac{7}{36} + \frac{1}{4} \times \frac{1}{6} = \frac{5}{216}, \epsilon = \frac{1}{3} \times \frac{5}{216} + \frac{1}{4} \times \frac{7}{36} = \frac{73}{1296}$$

the quotient is

$$1 - \frac{x}{6} + \frac{7x^2}{36} + \frac{5x^3}{216} + \frac{73x^4}{1296} + \dots$$

$$\begin{array}{r}
 1^{\circ} \quad \frac{a^2 - x(2a-b) - b^2}{ax + b^2} \\
 \hline
 a^3x - ax^2(2a-b) - ab^2x \\
 + a^2b^2 \quad - b^2x(2a-b) - b^4 \\
 \hline
 a^3x + a^2b^2 - ax^2(2a-b) - b^2x(2a-b) - b^4
 \end{array}$$

2^o In the dividend and divisor the powers of x and a, b occur in regular order

$$\begin{array}{r}
 1^{\circ} \quad \frac{a^2 - x(2a-b) - b^2}{ax + b^2} \\
 \hline
 a^3x - ax^2(2a-b) - ab^2x \\
 + a^2b^2 \quad - b^2x(2a-b) - b^4 \\
 \hline
 a^3x + a^2b^2 - ax^2(2a-b) - b^2x(2a-b) - b^4
 \end{array}$$

2^o Change the order of the divisor, thus $x + 2ab$: and proceed according the method: thus

$$\begin{array}{r}
 -2 \mid 3 + 3\alpha - 6 - 2\gamma \\
 \hline
 1 \mid \alpha + \beta + \gamma + \delta
 \end{array}$$

Since 3 makes α , we can find the value $\alpha, \beta, \gamma, \delta$ namely, $\alpha = 3, \beta = -2, \gamma = -2, \delta = 0$

\therefore the quotient is $3x^2 - 2ax + 2a^2b^2 + 0$.

3^o From the given condition;

$$\begin{cases} x^2 = 1 & xy = -2 \\ y^2 = 4 & yz = -6 \\ z^2 = 9 & xz = 3 \end{cases}$$

Apply the values of x, y, z , etc. in their proper place

$$3(1) - 2(-2) + 5(4) + 5(9) + 2(-6) + 2(3)$$

$$4(1) + 2(-2) + 3(4) + 2(9) + (-6) + (-3)$$

$$= \frac{66}{21} = 3\frac{1}{7} \text{ Ans.}$$

6. Apply the values of a , and b in the expression:

$$\begin{aligned}
 & x^{\frac{1}{2}}(-x-0)x^{\frac{3}{2}} + (x + (-x-0)0x-0 \\
 & = x^{\frac{1}{2}} + x^{\frac{3}{2}} + 0 - 0 = 2x^{\frac{1}{2}} = 2\left(\frac{1}{2}\right)^{\frac{1}{2}} \\
 & = \frac{2}{16} = \frac{1}{8}.
 \end{aligned}$$

7.

$$\begin{aligned}
 \frac{2x^3 - x^2 + x + 1}{2x^3 + 3x^2 + 3x + 1} &= \frac{(2x+1)(x^2-x+1)}{(2x+1)(x^2+x+1)} \\
 &= \frac{x^2-x+1}{x^2+x+1}.
 \end{aligned}$$

17th Grade

(Red circular stamp)

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